

HAT

8.3 Graphing Reciprocal Functions

1/17/18

Warm Up: Your family is driving 250 miles to Kansas City. How long will your trip take if your average speed is:

a. 60 mph? $\frac{250 \text{ miles}}{1} \cdot \frac{1 \text{ hour}}{60} = \frac{250}{60} = 4\frac{1}{6}$ 4 hrs. 10 min

b. 70 mph? $\frac{250}{70} = 3\frac{4}{7} \approx 3 \text{ hrs } 34 \text{ min}$ 60 miles

c. 45 mph? $\approx 5 \text{ hrs } 33 \text{ min}$

d. 10 mph? $\frac{250}{10} = 25 \text{ hours}$

Write an equation to represent the time of the trip T , given the average speed, S .

$$T = \frac{D}{S}$$

Theoretical Domain vs. Practical Domain

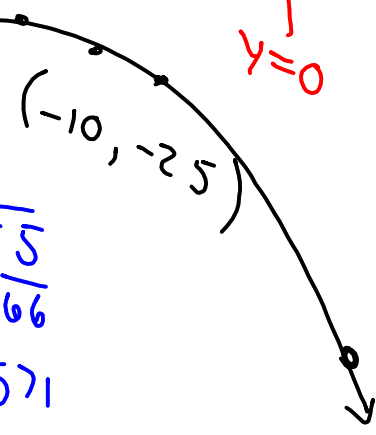
$$s \in \mathbb{R} \\ s \neq 0$$

$$D: \{s \mid s \in (-\infty, 0) \cup (0, \infty)\}$$

$$T = \frac{D}{s}$$

$$T = \frac{250}{s}$$

S	T
10	25
45	5.55
60	4.166
>0	3.571



Practical
 $D: \{s \mid s \in (0, \infty)\}$
 What makes sense
 in context of
 the problem

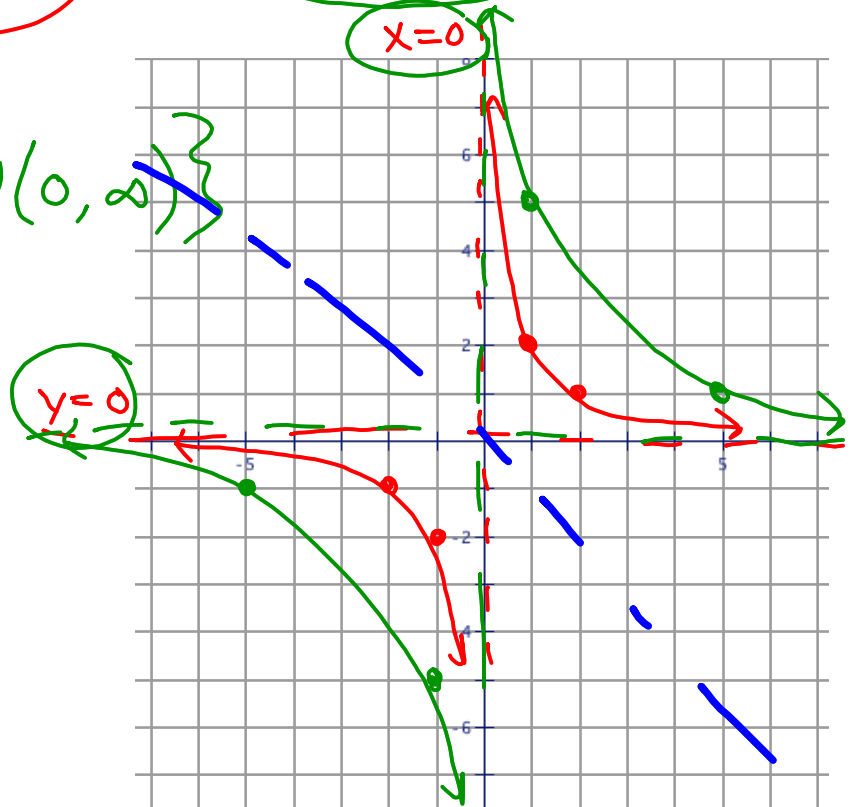
For each example:

- a. Sketch the graph.
- b. State the domain and range.
- c. Write equations for all asymptotes.

Ex#1: $f(x) = \frac{2}{x}$

$g(x) = \frac{5}{x}$

$D: \{x \mid x \in (-\infty, 0) \cup (0, \infty)\}$

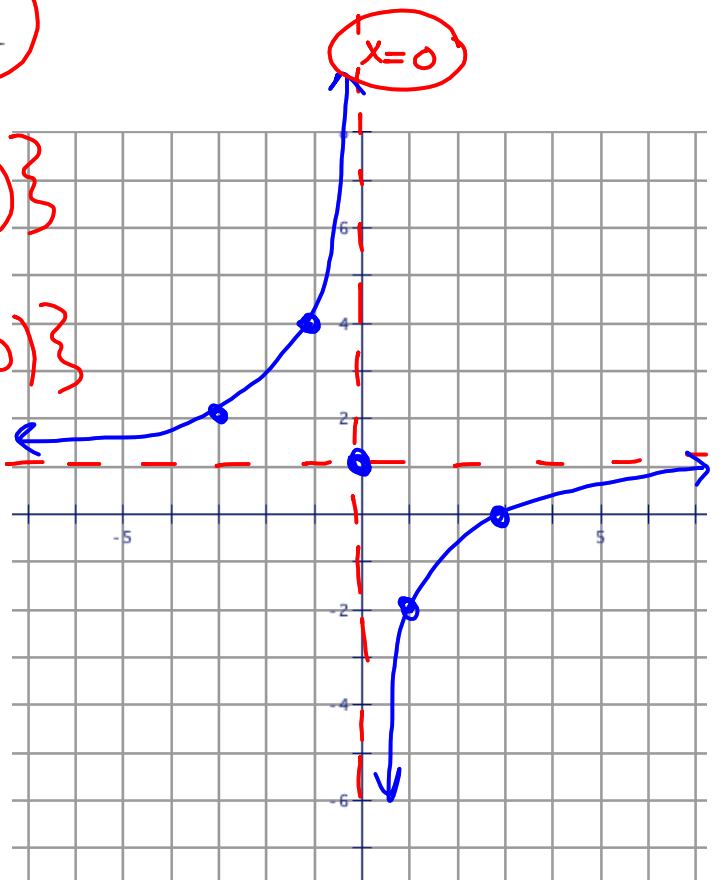


Ex#2: $f(x) = \frac{-3}{x} + 1$ H.A.

$\mathcal{D}: \{x \mid x \in (-\infty, 0) \cup (0, \infty)\}$

$\mathcal{R}: \{y \mid y \in (-\infty, 1) \cup (1, \infty)\}$

$y=1$



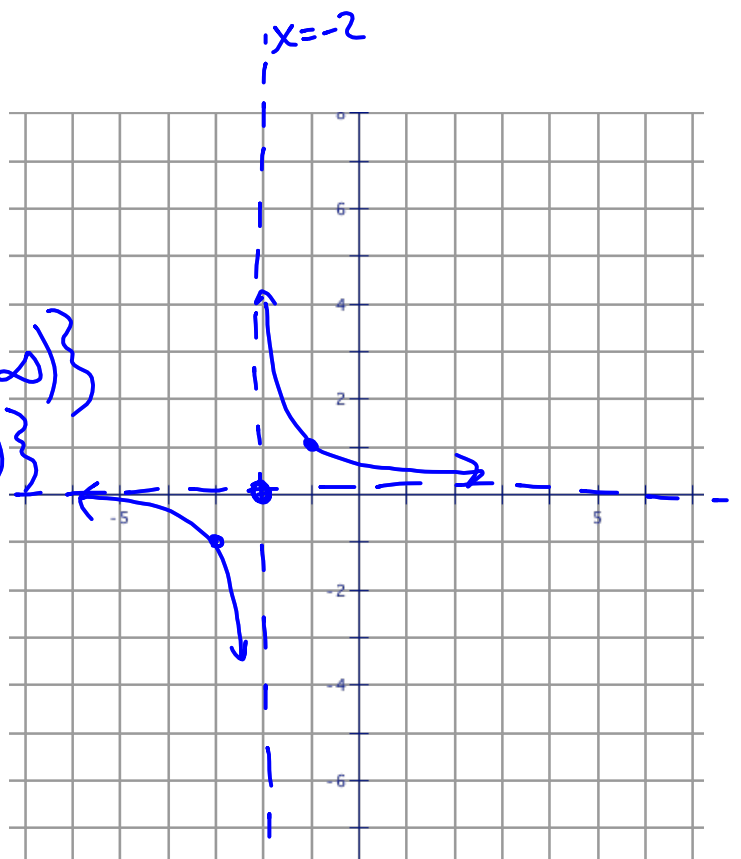
Ex#3: $f(x) = \frac{1}{x+2}$
 $= \frac{1}{x}$

$D: \{x \mid x \in (-\infty, -2) \cup (-2, \infty)\}$

$R: \{y \mid y \in (-\infty, 0) \cup (0, \infty)\}$

$x = -2$

$y = 0$



Ex#4: $f(x) = \frac{2}{x-1} - 4$

stretch 2 ← 2

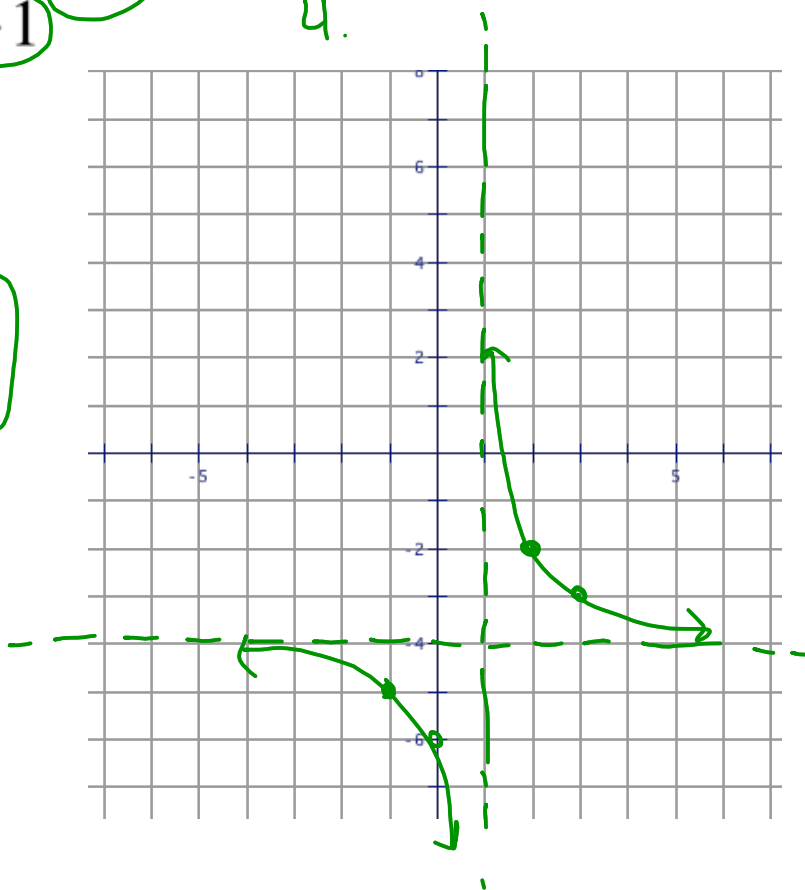
shift down 4.

shift right 1

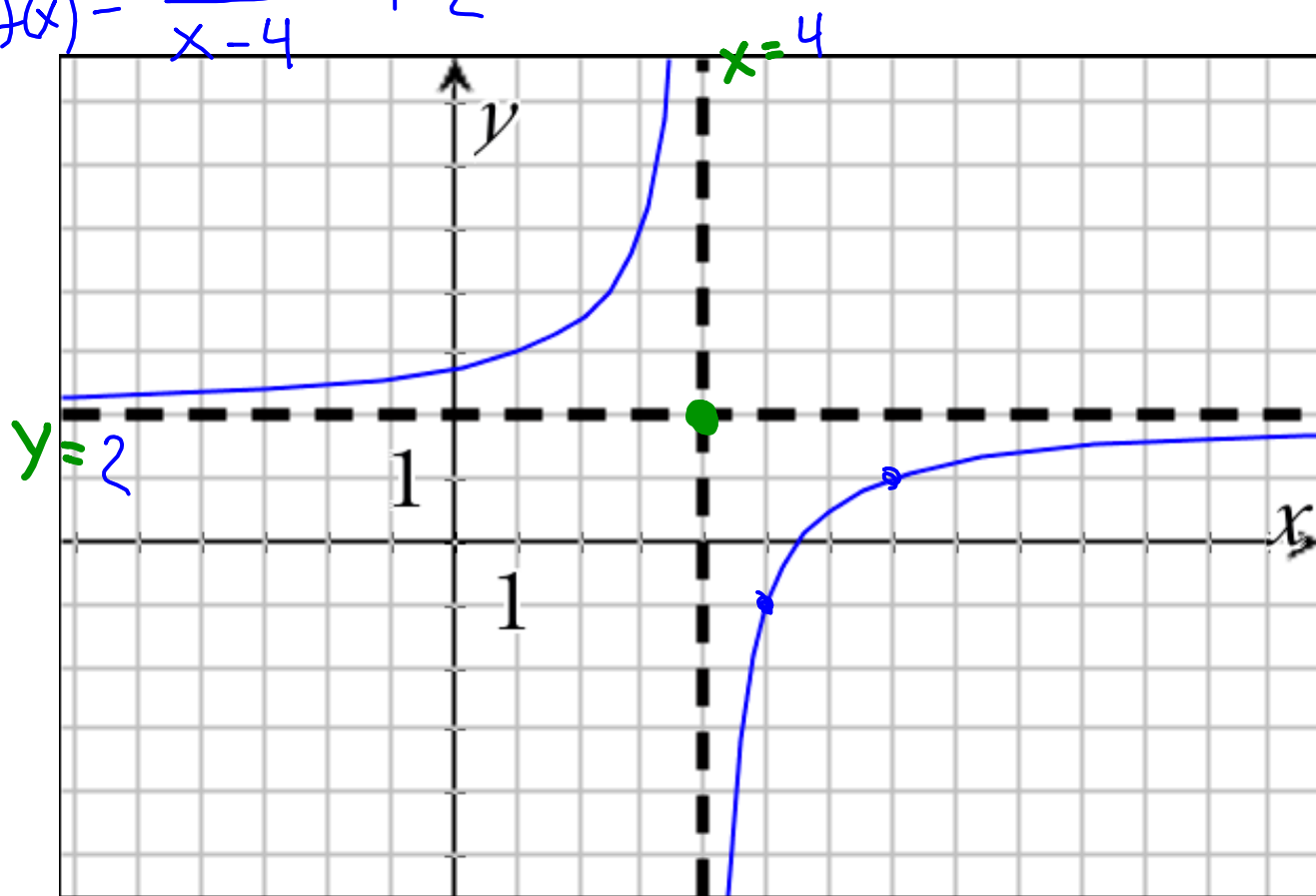
$$f(x) = \frac{2}{x}$$

$$x = 1$$

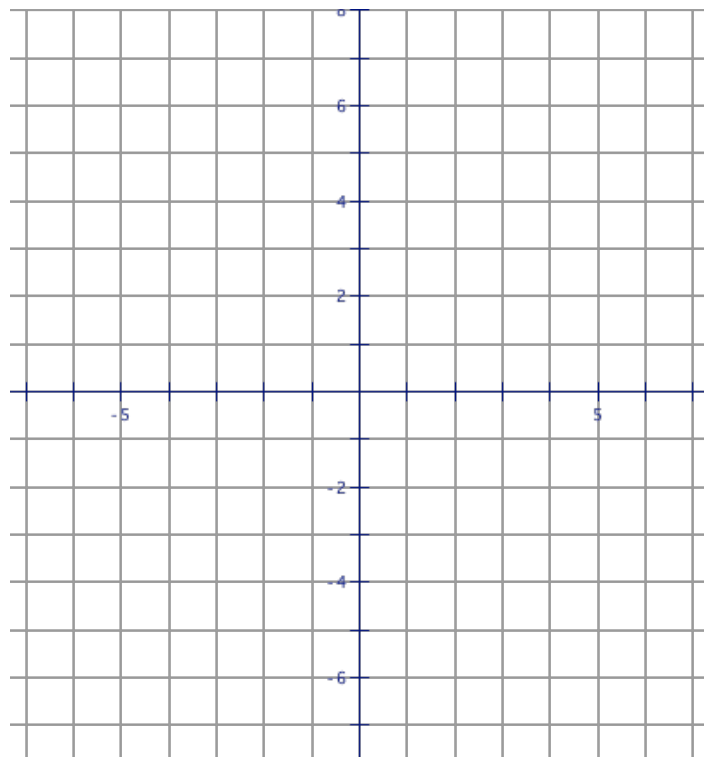
$$y = -4$$



$$f(x) = \frac{-3}{x-4} + 2$$



Ex#5: Graph $f(x) = \frac{x+2}{x-1}$



Assignment:

page 548 #9, 15, 17, 21, 23, 25, 29, 38, 41